## **CHAPTER 8**

## **APPLICATIONS OF INTEGRALS**

## LONG ANSWER TYPE QUESTIONS (6 MARKS)

1. Find the area enclosed by circle  $x^2 + y^2 = a^2$ .

2. Find the area of region bounded by  $\left\{ (x, y) : |x - 1| \le y \le \sqrt{25 - x^2} \right\}$ .

- 3. Find the area enclosed by the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$
- 4. Find the area of region in the first quadrant enclosed by x-axis, the line y = x and the circle  $x^2 + y^2 = 32$ .
- 5. Find the area of region  $\{(x, y) : y^2 \le 4x, 4x^2 + 4y^2 \le 9\}$
- 6. Prove that the curve  $y = x^2$  and,  $x = y^2$  divide the square bounded by x = 0, y = 0, x = 1, y = 1 into three equal parts.

7. Find smaller of the two areas enclosed between the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ and the line

bx + ay = ab.

- 8. Find the common area bounded by the circles  $x^2 + y^2 = 4$  and  $(x 2)^2 + y^2 = 4$ .
- 9. Using integration, find the area of the region bounded by the triangle whose vertices are
  - (a) (-1, 0), (1, 3) and (3, 2) (b) (-2, 2) (0, 5) and (3, 2)
- 10. Using integration, find the area bounded by the lines.
  - (i) x + 2y = 2, y x = 1 and 2x + y 7 = 0
  - (ii) y = 4x + 5, y = 5 x and 4y x = 5.
- 11. Find the area of the region  $\{(x, y) : x^2 + y^2 \le 1 \le x + y\}$ .
- 12. Find the area of the region bounded by

$$y = |x - 1|$$
 and  $y = 1$ .

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- 13. Find the area enclosed by the curve  $y = \sin x$  between x = 0 and  $x = \frac{3\pi}{2}$  and *x*-axis.
- 14. Find the area bounded by semi circle  $y = \sqrt{25 x^2}$  and x-axis.
- 15. Find area of region given by  $\{(x, y) : x^2 \le y \le |x|\}$ .
- 16. Find area of smaller region bounded by ellipse  $\frac{x^2}{9} + \frac{y^2}{4} = 1$  and straight line 2x + 3y = 6.
- 17. Find the area of region bounded by the curve  $x^2 = 4y$  and line x = 4y 2.
- 18. Using integration find the area of region in first quadrant enclosed by x-axis, the line  $x = \sqrt{3}y$  and the circle  $x^2 + y^2 = 4$ .
- 19. Find smaller of two areas bounded by the curve y = |x| and  $x^2 + y^2 = 8$ .
- 20. Find the area lying above x-axis and included between the circle  $x^2 + y^2 = 8x$  and the parabola  $y^2 = 4x$ .
- 21. Using integration, find the area enclosed by the curve  $y = \cos x$ ,  $y = \sin x$  and x-axis in the interval  $\left(0, \frac{\pi}{2}\right)$ .
- 22. Sketch the graph y = |x 5|. Evaluate  $\int_0^6 |x 5| dx$ .
- 23. Find area enclosed between the curves, y = 4x and  $x^2 = 6y$ .
- 24. Using integration, find the area of the following region :

$$\left\{\left(x, y\right): \left|x-1\right| \leq y \leq \sqrt{5-x^2}\right\}$$

## ANSWERS

- 1.  $\pi a^2$  sq. units.
- 2.  $\left(25\frac{\pi}{4} \frac{1}{2}\right)$  sq. units. 3.  $\pi ab$  sq. units 5.  $\frac{\sqrt{2}}{6} + \frac{9\pi}{8} - \frac{9}{8}\sin^{-1}\left(\frac{1}{3}\right)$  sq. units 7.  $\frac{(\pi - 2)ab}{4}$  sq. units
- 8.  $\begin{pmatrix} 8\pi & 2\sqrt{3} \\ 3 & 2\sqrt{3} \end{pmatrix}$  sq. units 9. (a) 4 sq. units (b) 2 sq. units
- 10. (a) 6 sq. unit [Hint. Coordinate of vertices are (0, 1) (2, 3) (4, -1)]

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(b) 
$$\frac{15}{2}$$
 sq. [Hint : Coordinate of vertices are (-1, 1) (0, 5) (3, 2)]  
11.  $\left(\frac{\pi}{4} - \frac{1}{2}\right)$  sq. units  
12. 1 sq. units  
13. 3 sq. units  
14.  $\frac{25}{2}\pi$  sq. units  
15.  $\frac{1}{3}$  sq. units  
16.  $\frac{3}{2}(\pi - 2)$  sq. units  
17.  $\frac{9}{8}$  sq. units  
18.  $\frac{\pi}{3}$  sq. unit  
19.  $2\pi$  sq. unit.  
20.  $\frac{4}{3}(8 + 3\pi)$  sq. units  
21.  $(2 - \sqrt{2})$  sq. units.  
22. 13 sq. units.  
23. 8 sq. units.  
24.  $\left(\frac{5\pi}{4} - \frac{1}{2}\right)$  sq. units

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